



CS 329P : Practical Machine Learning (2021 Fall)

5.4 Stacking

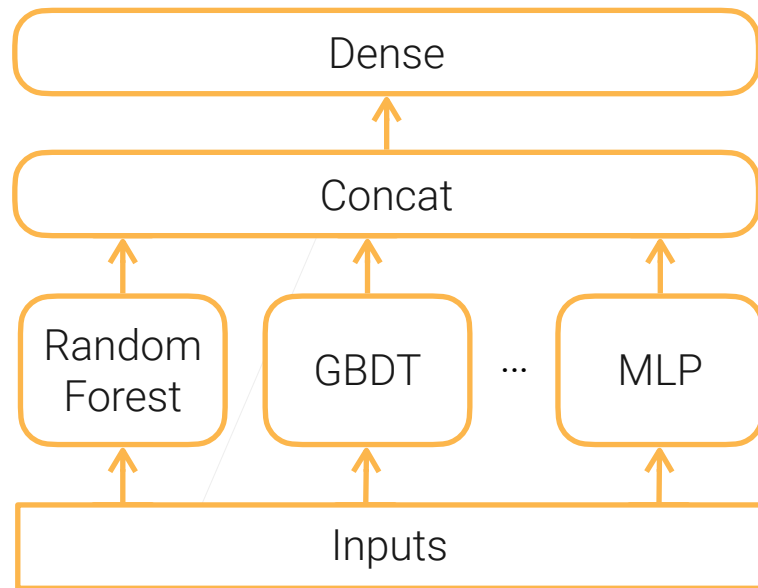
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<https://c.d2l.ai/stanford-cs329p>

Stacking



- Combine multiple base learners to reduce variance
 - Base learners can be different model types
 - Linearly combine base learners outputs by learned parameters
- Widely used in competitions
- bagging VS stacking
 - Bagging: bootstrap samples to get diversity
 - Stacking: different types of models extract different features



Stacking Results



- Evaluate on house sales data, compare to bagging and GBDT we implemented before

	Test Error
GBDT	0.259
RandomForest	0.243
Stacking (AutoGluon)	0.229

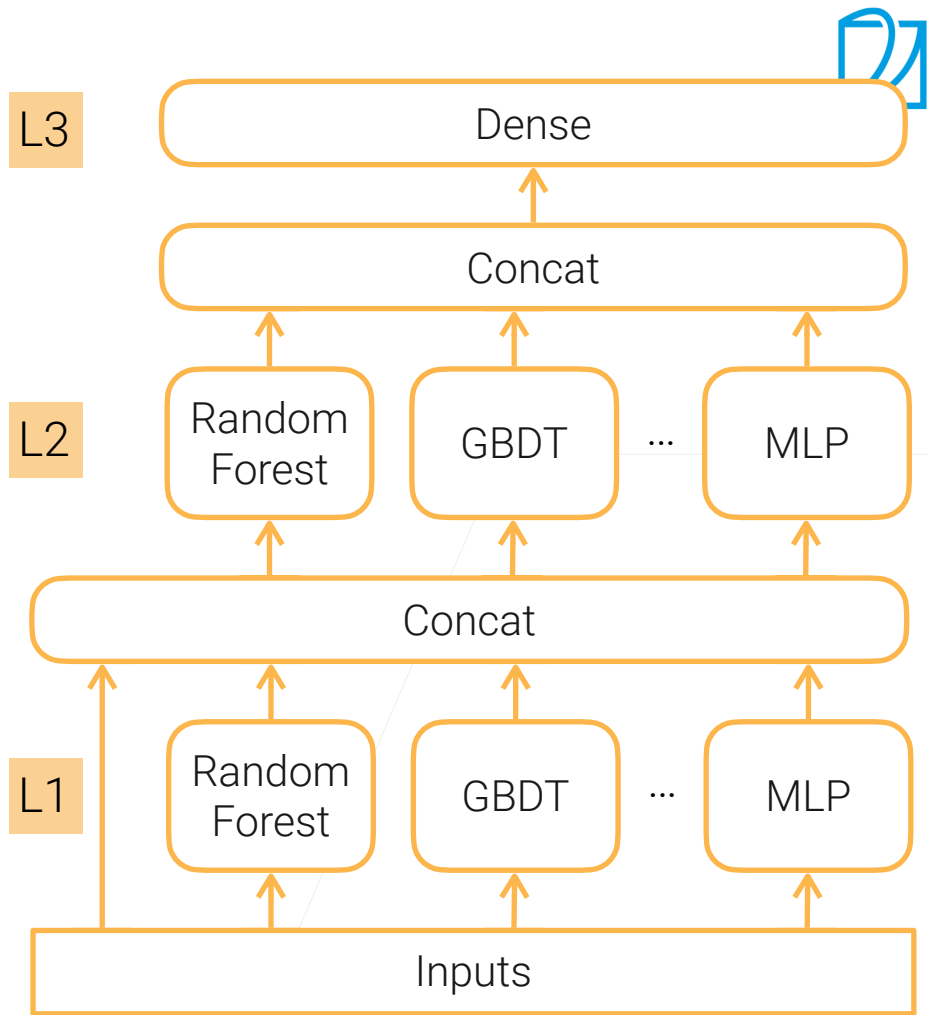
	model	score_test	score_val	pred_time_test
0	WeightedEnsemble_L2	-0.229626	-0.222406	3.953961
1	ExtraTrees	-0.232468	-0.232027	1.831407
2	CatBoost	-0.238690	-0.230338	0.016279
3	LightGBM	-0.239441	-0.226900	0.203499
4	NeuralNetMXNet	-0.241847	-0.246979	4.397190
5	RandomForest	-0.242904	-0.234931	1.750319
6	XGBoost	-0.249837	-0.240684	0.086715
7	KNeighbors	-0.457131	-0.443591	0.107212

```
from autogluon.tabular import TabularPredictor

predictor = TabularPredictor(label=label).fit(train)
```

Multi-layer Stacking

- Stacking base learners in multiple levels to reduce bias
 - Can use a different set of base learners at each level
- Upper levels (e.g. L2) are trained on the outputs of the level below (e.g. L1)
 - Concatenating original inputs helps



Overfitting in Multi-layer Stacking



- Train learners from different levels on different data to alleviate overfitting
 - Split training data into A and B , train L1 learners on A , run inference on B to generate training data for L2 learners
- Repeated k -fold bagging:
 - Train k models as in k -fold cross validation
 - Combine predictions of each model on out-of-fold data
 - Repeat step 1,2 by n times, average the n predictions of each example for the next level training

Multi-layer Stacking Results



- Use 1 additional stacked level, with 5-fold repeated bagging
 - Error: 0.229 \rightarrow 0.227
 - Training time: 39 sec \rightarrow 207 sec (5x)

```
from autogluon.tabular import TabularPredictor  
  
predictor = TabularPredictor(label=label).fit(  
    train, num_stack_levels=1, num_bag_folds=5)
```

	model	score_test	score_val
0	NeuralNetMXNet_BAG_L2	-0.225332	-0.219718
1	WeightedEnsemble_L3	-0.226921	-0.216254
2	CatBoost_BAG_L2	-0.227525	-0.217471
3	WeightedEnsemble_L2	-0.228386	-0.218298
4	LightGBM_BAG_L2	-0.228400	-0.218374
5	XGBoost_BAG_L2	-0.228660	-0.218824
6	ExtraTrees_BAG_L2	-0.228751	-0.217563
7	ExtraTrees_BAG_L1	-0.233527	-0.224974
8	RandomForest_BAG_L2	-0.234270	-0.220346
9	CatBoost_BAG_L1	-0.237356	-0.227126
10	LightGBM_BAG_L1	-0.238102	-0.225848
11	NeuralNetMXNet_BAG_L1	-0.238413	-0.238786
12	XGBoost_BAG_L1	-0.241698	-0.235570
13	RandomForest_BAG_L1	-0.242029	-0.227800
14	KNeighbors_BAG_L1	-0.457909	-0.447980

Model Combination Summary



Reduce	Bias	Variance	Computation Cost	Parallelization
Bagging	-	Y	n	n
Boosting	Y	-	n	1
Stacking	-	Y	n	n
K-fold multi-level stacking	Y	Y	$nlxk$	nxk

n : number of learners, l : number of levels, k : k-fold